

# The Ninth Grade Math Competition Class

## Logarithm Challenging Problems

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0. What is the logarithm of  $27\sqrt[4]{9}\sqrt[3]{9}$  base 3?

1. Find  $x$  if  $\log_9(2x - 7) = \frac{3}{2}$ .

2. Find  $\log_{\sqrt{3}} \sqrt[3]{9}$ .

3. Solve the equation  $\log_{2x} 216 = x$ , where  $x$  is real.

4. Find base  $b$  such that  $\log_b 5\sqrt{5} = \frac{5}{2}$ .

5. If  $\log_2 b - \log_2 a = 3$ , then  $b^2 - a^2 = Ma^2$ , compute  $M$ .

6. If  $\frac{\log_b a}{\log_c a} = \frac{19}{99}$ ,  $\frac{b}{c} = c^k$ , find the value of  $k$ .

7. Let  $T = 1.8$ , compute base  $b$  if  $\log_b(75T) = 2 + \log_b 3 + \log_b 5$ .



**8.** If  $\log_{225} x + \log_x 15 = \frac{11}{6}$ , find  $x$ .

9. Evaluate  $\frac{1}{\log_2 \frac{1}{6}} - \frac{1}{\log_3 \frac{1}{6}} - \frac{1}{\log_4 \frac{1}{6}}$

10. Compute the value of  $n$  for which  $\frac{1}{\log_2 100} + \frac{1}{\log_3 100} + \frac{1}{\log_6 100} + \frac{1}{\log_9 100} = \frac{2}{\log_N 100}$ .

11. Given the points  $A (\log 2, \log 3)$  and  $B (\log(\log T^2), \log(\log T^3))$ , compute the slope of the line  $\overleftrightarrow{AB}$ .

12. Given that  $\log_6 a + \log_6 b + \log_6 c = 6$ , and  $a, b, c$  are positive integers that form an increasing geometric sequence and  $b - a$  is the square of an integer. Find  $a + b + c$ .